



MAX PLANCK INSTITUTE  
FOR SOFTWARE SYSTEMS



# On the Existence of a Cyclic Schedule for Non-Preemptive Periodic Tasks with Release Offset

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# Motivations



Scheduling table is stored  
in **memory**

Consumes energy  
and space

Increases the total  
production cost



## Arm Cortex MCU family

Total Parts: (752) for STM32 32-bit ARM Cortex MCUs   Matching Parts : (90)						
Part Number	Package	Core	Operating Frequency (MHz) (Processor speed)	FLASH Size (kB) (Prog)	Internal RAM Size (kB)	I/Os (High Current)
STM32L011G4	UFQFPN 28 4x4 x0.55	ARM Cortex-M...	32	16	2	24
STM32L011K4	LQFP 32 7x7x1.4	ARM Cortex-M...	32	16	2	28
STM32L021D4	TSSOP 14	ARM Cortex-M...	32	16	2	11
STM32L021F4	UFQFPN 20 3x3 x0.6	ARM Cortex-M...	32	16	2	16
STM32L021G4	UFQFPN 28 4x4 x0.55	ARM Cortex-M...	32	16	2	24
STM32L021K4	LQFP 32 7x7x1.4	ARM Cortex-M...	32	16	2	28
STM32L031F4	TSSOP 20	ARM Cortex-M...	32	16	8	15
STM32L071C8	LQFP 48 7x7x1.4	ARM Cortex-M...	32	64	20	37
STM32L071R2	LQFP 64 10x10 x1.4	ARM Cortex-M...	32	192	20	51
STM32L071VB	LQFP 100 14x14 x1.4	ARM Cortex-M...	32	128	20	84

# Finding an Observation Interval for Online Algorithms

## System model and assumptions

- Uniprocessor
- **Non-preemptive**
- Periodic tasks
- Constrained deadline
- Independent tasks

We are interested in the approaches that build the table using an online algorithm

- **What is the length of cyclic schedule?**
  - **Synchronous release:** one hyperperiod
  - **Asynchronous release:** depends on the scheduling algorithm



Work-conserving or  
Non-work-conserving?

# State-of-the-Art of Simulation Interval

Processor	Deadlines	Dependency	Scheduling algorithm	Simulation interval	Reference
1	$D_i \leq T_i$	Independent	Fixed-task priority	$[0, O^{\max} + 2H)$	Leung and Merrill (1980)
1	Arbitrary	Independent	Fixed-job priority	$[0, O^{\max} + 2H)$	Goossens and Devillers (1999)
1	$D_i \leq T_i$	Independent	Fixed-job priority	$[0, S_n + H)$	Goossens and Devillers (1997)
1	$D_i \leq T_i$	Mutual exclusion, simple precedence	Any work-conserving (with idle task)	$[0, \theta_c + H)$	Choquet-Geniet and Grolleau (2004), Bado et al. (2012)
Uniform	$D_i \leq T_i$	Independent	Global fixed-task priority	$[0, S_n + H)$	Cucu and Goossens (2006)
Unrelated	$D_i \leq T_i$	Independent	Global fixed-task priority	$[0, S_n + H)$	Cucu-Grosjean and Goossens (2011)
Identical	Arbitrary	Independent	Global fixed-task priority	$[0, \hat{S}_n + H)$	Cucu and Goossens (2007)
Identical	$D_i \leq T_i$	Independent	Any	$[0, O^{\max} + H \prod_{i=1}^n (C_i + 1))$	Baro et al. (2012), Nélis et al. (2013)
Identical	$D_i \leq T_i$	Simple precedence	Any	$[0, O^{\max} + H \prod_{i=1}^n (C_i + 1))$	Baro et al. (2012)
Identical	Arbitrary	Structural constraint	Any	$[0, H \prod_{i=1}^n ((O_i + D_i - T_i)_0 + 1))$	Goossens et al. (2016)

**Impractical!**

$$\hat{s}_1 \doteq O_1$$

$$\hat{s}_i \doteq \max \left( O_i, O_i + \left\lceil \frac{\hat{s}_{i-1} - O_i}{T_i} \right\rceil T_i \right) + H_i$$

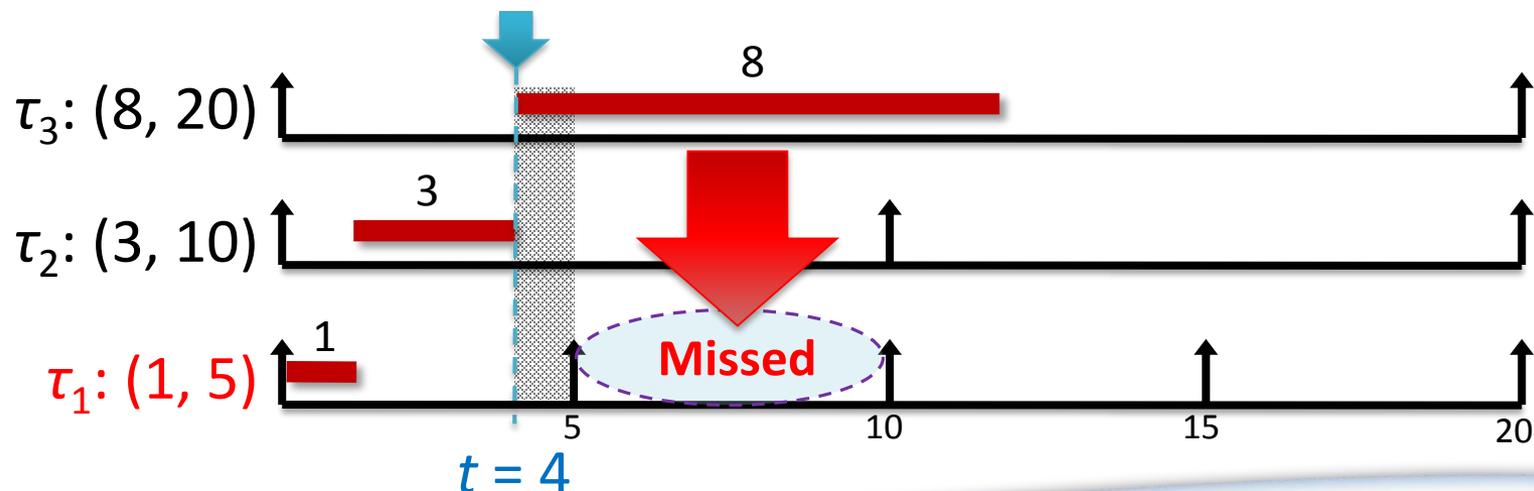
$$H_i \doteq \text{lcm}_{j=1 \dots i} (T_j)$$

$$[0, H \prod_{i=1}^n ((O_i + D_i - T_i)_0 + 1))$$

J. Goossens, E. Grolleau, L. Cucu-Grosjean, Periodicity of real-time schedules for dependent periodic tasks on identical multiprocessor platforms, Real-Time Systems, 2016.

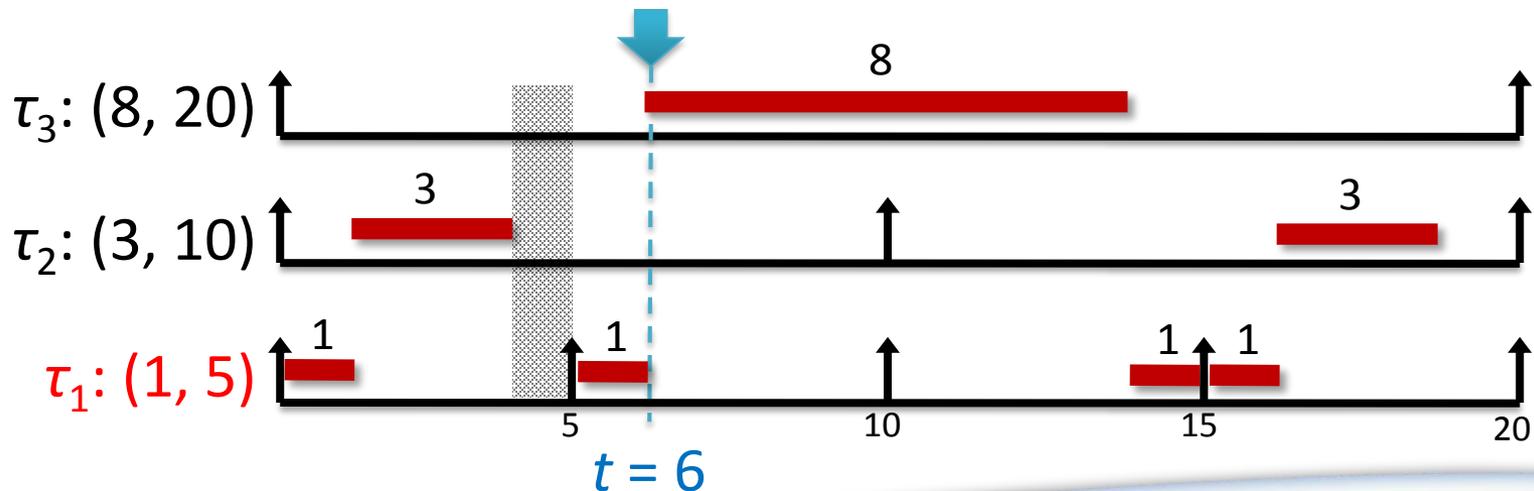
# Non-Work-Conserving Scheduling

- ▶ Leaves the processor idle even if there are tasks that are not yet scheduled
- ▶ Example: **Precautious-RM** [Nasri2014]
  - is an online algorithm
  - follows rate monotonic priorities
  - schedules the highest-priority task only if it will not cause a deadline miss for the next job of the task with the smallest period

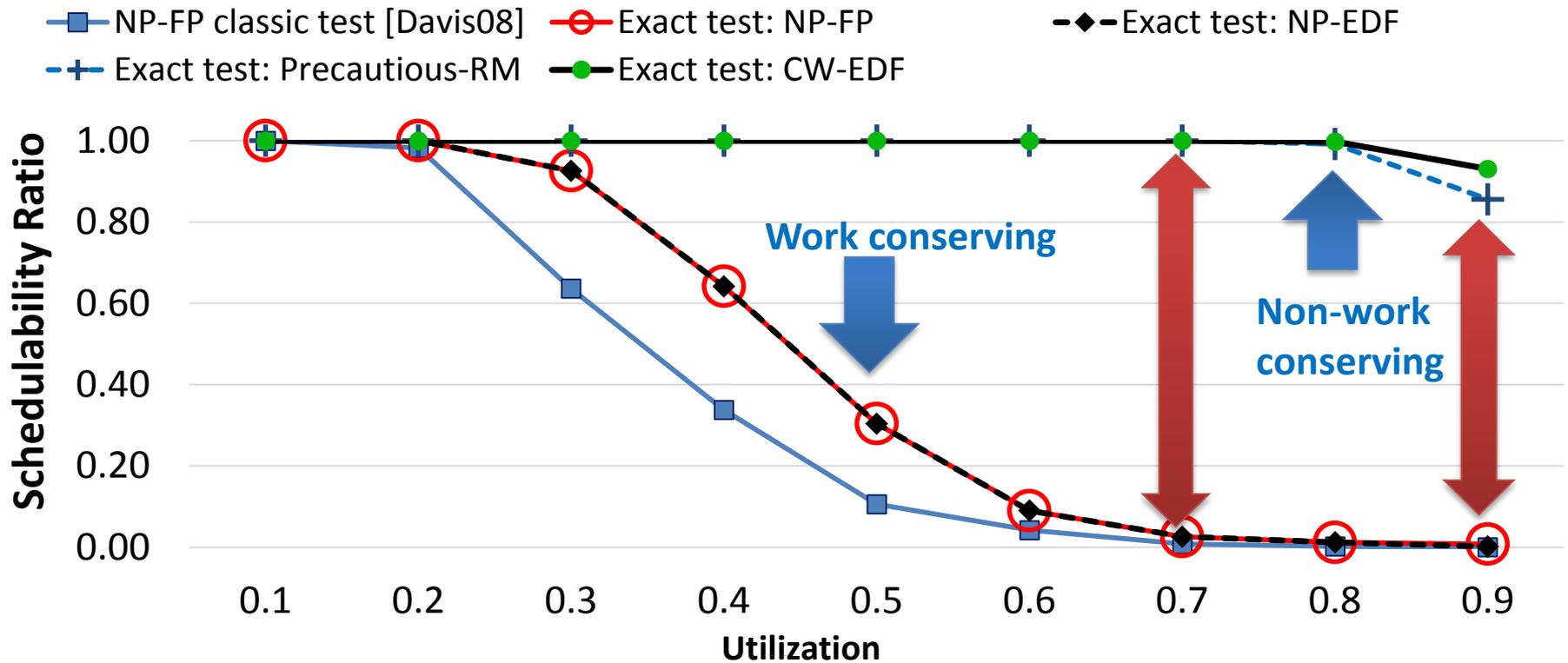


# Non-Work-Conserving Scheduling

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# Why Non-Work-Conserving Algorithms are Needed?



- Autosar benchmark [Kramer2015] (only task set that satisfy the “necessary schedulability conditions”).
- The exact test is from Nasri and Brandenburg, “An Exact and Sustainable Analysis of Non-Preemptive Scheduling”, manuscript, available at [https://people.mpi-sws.org/~bbb/papers/pdf/preprint\\_np\\_exact\\_analysis.pdf](https://people.mpi-sws.org/~bbb/papers/pdf/preprint_np_exact_analysis.pdf)

# Problem 1

## ▶ Given:

- Uniprocessor
- Non-preemptive
- Periodic tasks
- Release offsets
- Constrained (or arbitrary) deadline
- Dependent (or independent)

## ▶ Scheduled by:

- A **non-work-conserving** scheduling algorithm such as Precautious-RM

## ▶ Problem:

**What is the length of a cyclic schedule?**

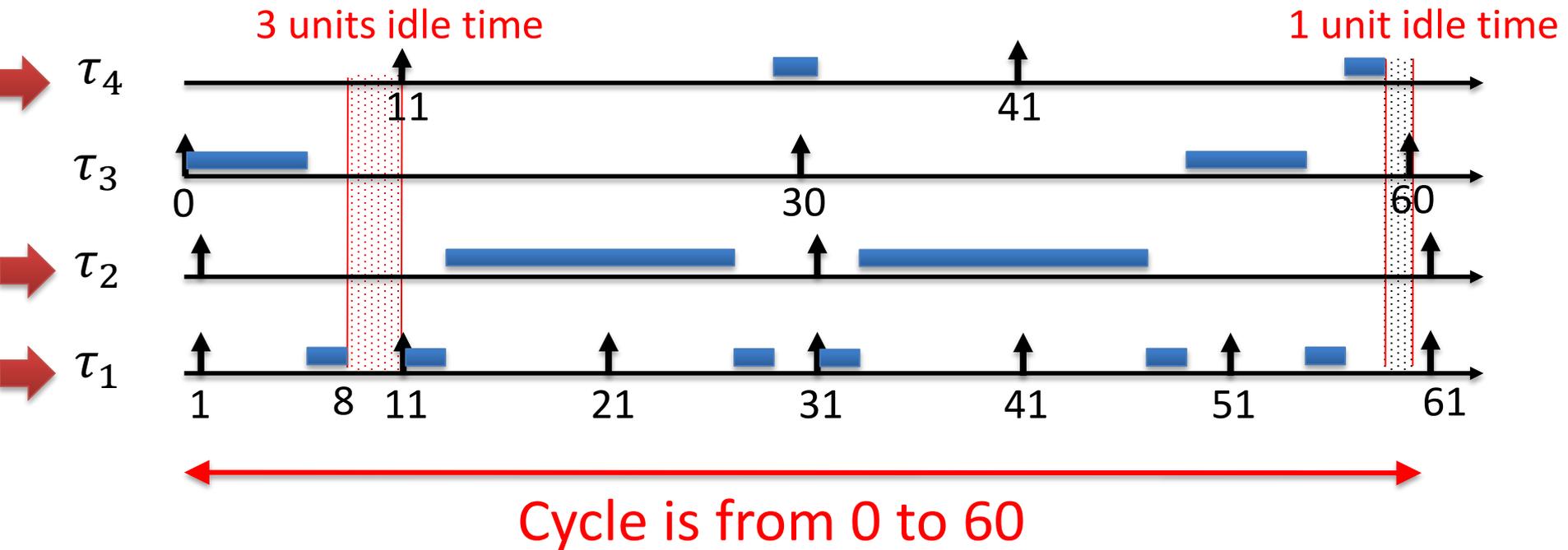
**When does the cyclic schedule start?**

# The Length of Cyclic Schedule

Hyperperiod is 30.

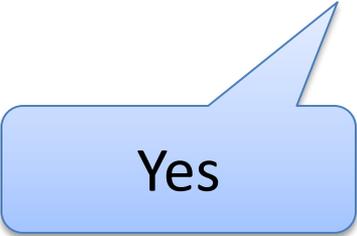
$\tau_i$	$C_i$	$D_i$	$T_i$	$O_i$
$\tau_1$	2	10	10	1
$\tau_2$	14	30	30	1
$\tau_3$	6	30	30	0
$\tau_4$	2	30	30	11

Precautious-RM schedule:

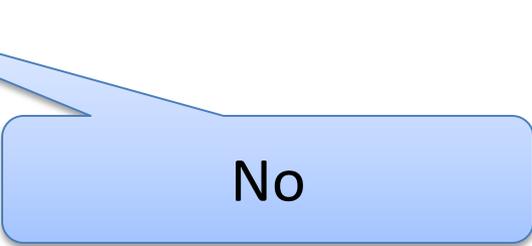


# Other Open Problems

- ▶ **Problem 3: Is there any feasible asynchronous task set  $\tau$  that does not have any cyclic schedule with length  $H$ ?**



Yes



No

## Problem 4:

**Given:** a feasible non-preemptive task set

**Find:** schedule  $S$  that has the smallest cycle length

## Problem 5:

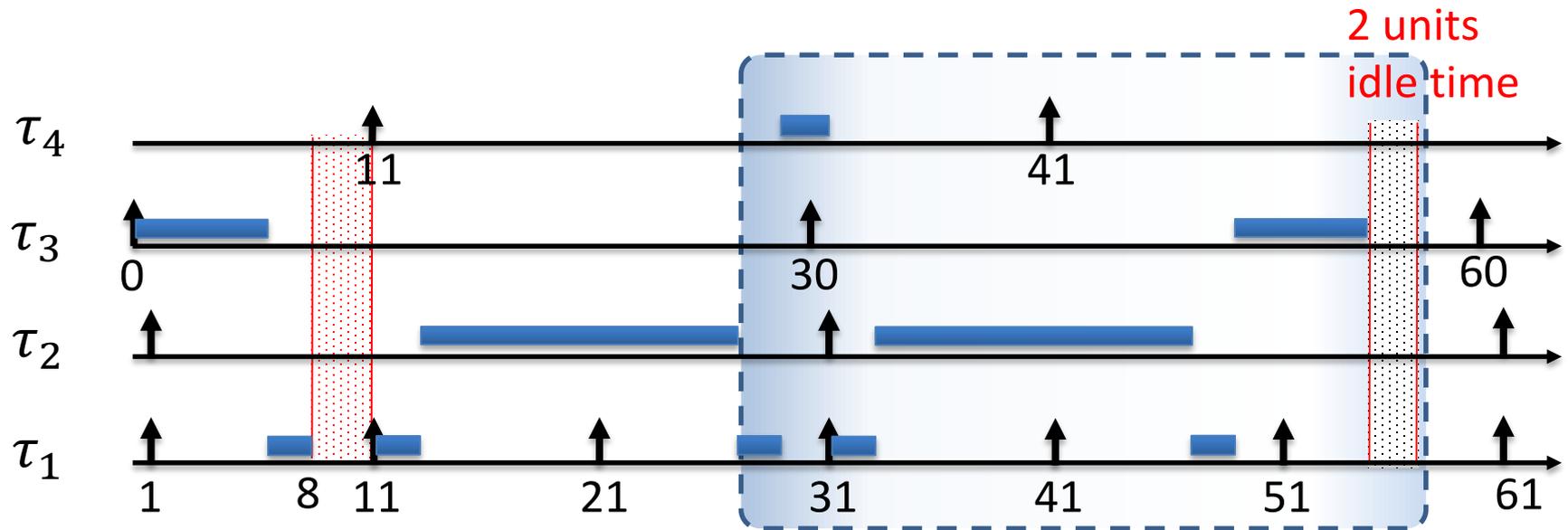
**Given:** a feasible non-preemptive task set

**Find:** How to find/build that schedule?

$H$  = hyperperiod

**Assume:** task set is periodic with constrained deadline and independent tasks

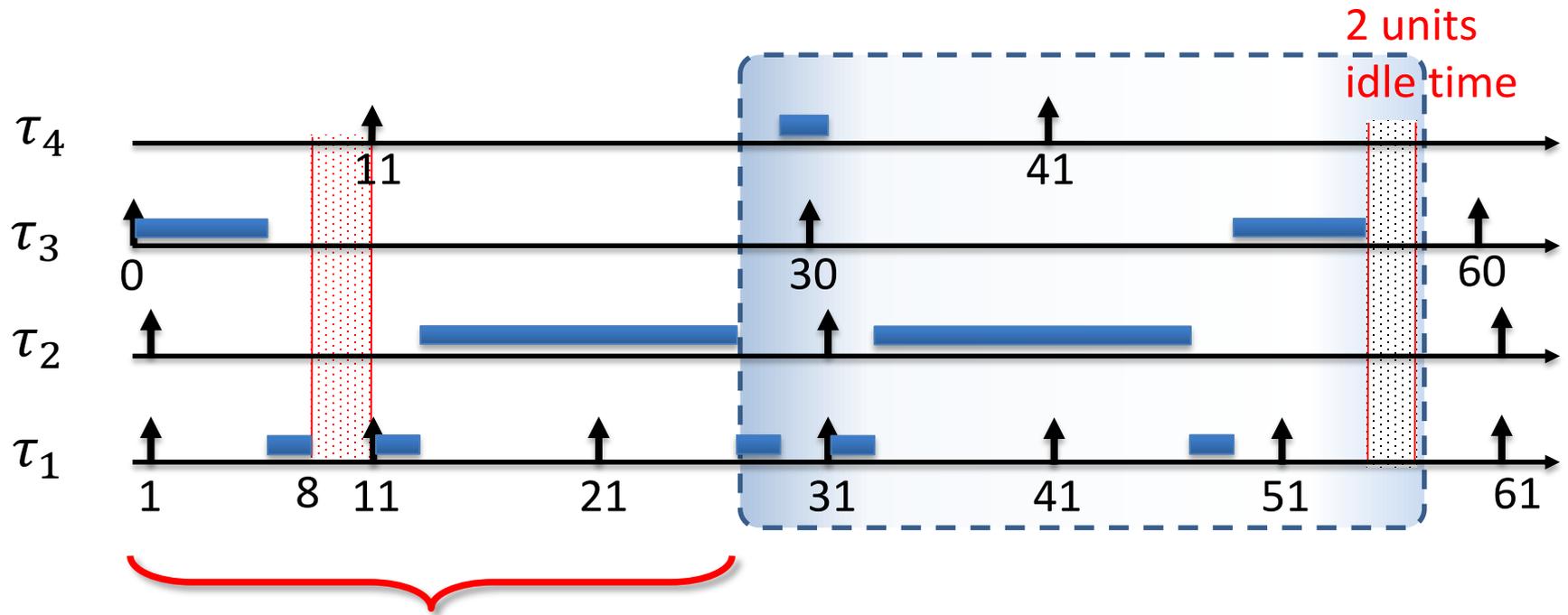
# Find a Cyclic Schedule with Length H



**A cyclic schedule with length H exists.**

Hyperperiod =  $H = 30$

# Other Concerns



**What about the length of non-cyclic schedule?  
What if it is even larger than the cyclic schedule?**

Hyperperiod =  $H = 30$

# Summary



Small offline tables

## Motivations

- The need of creating small offline tables to save memory
- Using online scheduling algorithms is an efficient option



Performance and predictability

## Non-work-conserving non-preemptive scheduling

- Promising performance
- High system predictability



The length and start time of a cyclic schedule

## Open Problems

- No practical bound on the length of simulation interval
- We need methods to find the smallest cyclic schedule



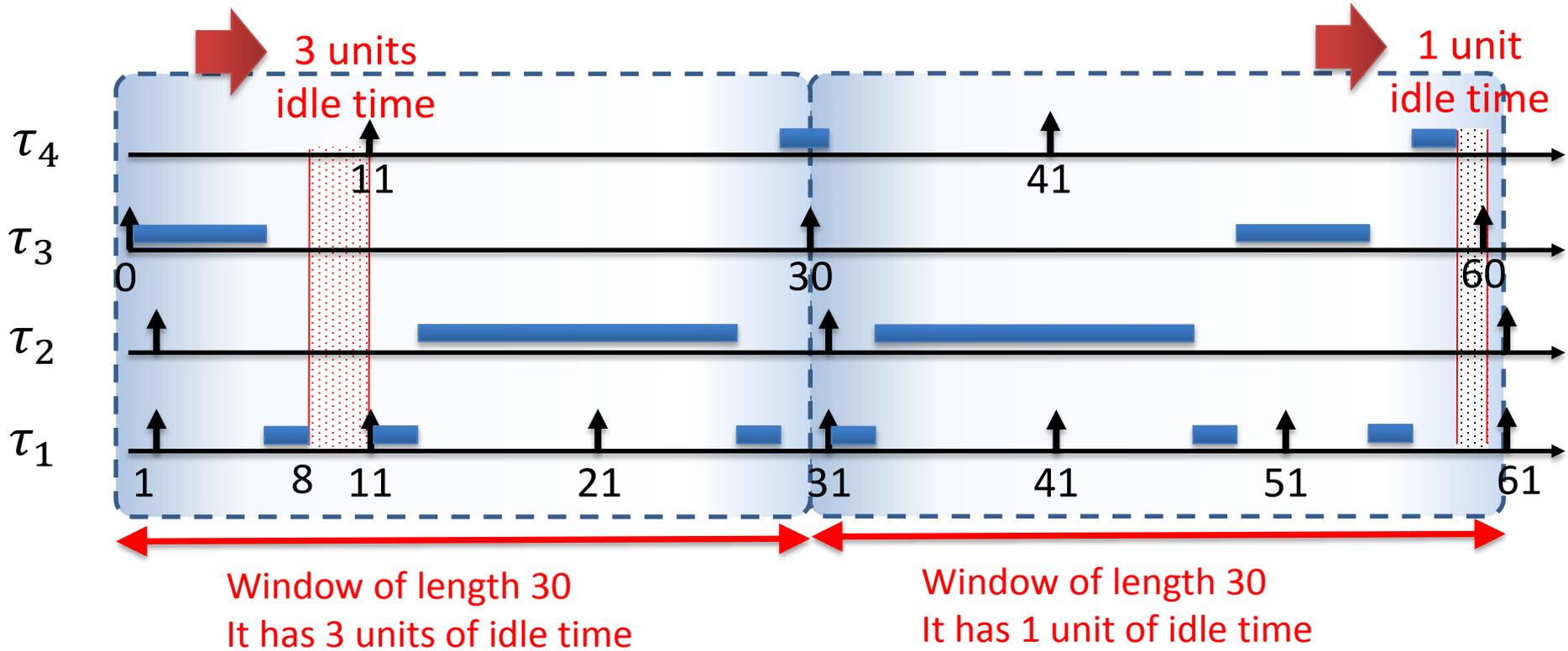
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Thank you



# Looking Closer



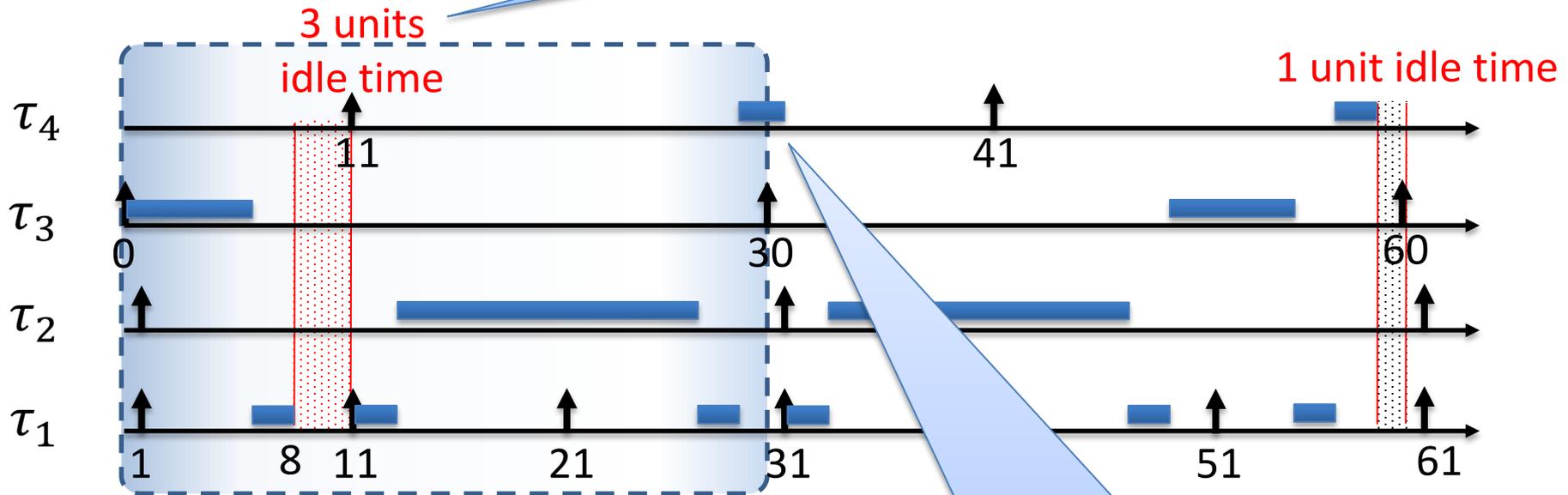
- Hyperperiod = 30
- $U = 28/30$
- Slack in hyperperiod =  $(1-U)H = 2$

This window is **borrowing** slack from the next one

# Find a Cyclic Schedule with Length H

**One solution:** Sliding Observation Window

It has more than 2 units of slack

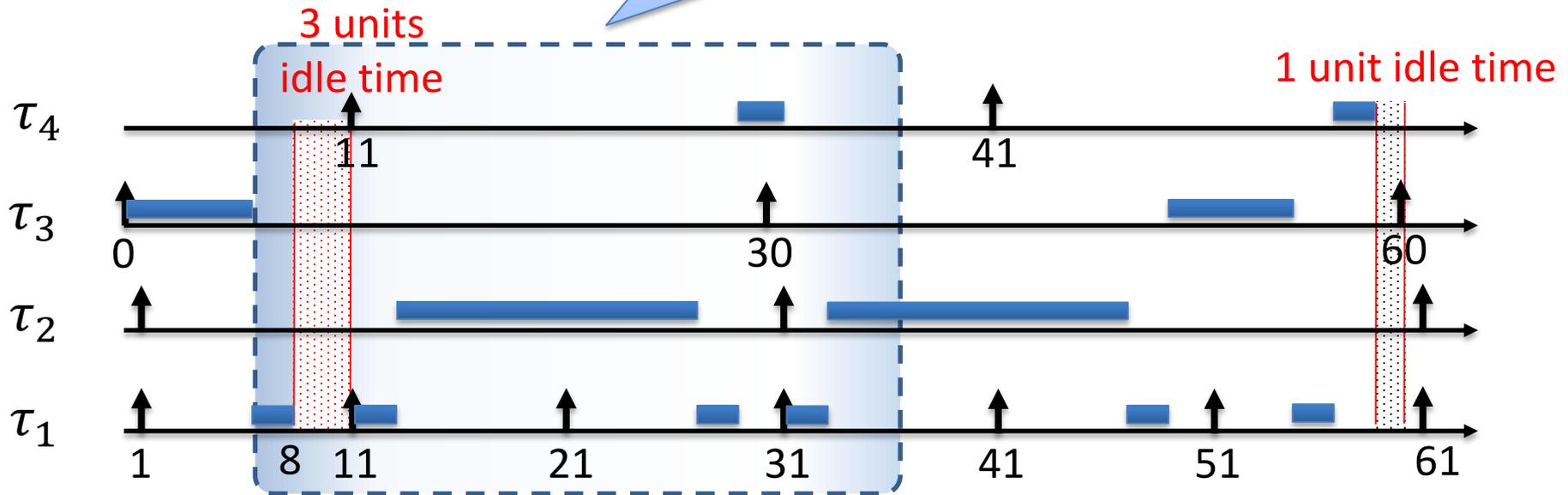


Cannot be a cyclic schedule because  $\tau_2$  has not been finished within the window

Hyperperiod =  $H = 30$   
 $U = 28/30$

# Find a Cyclic Schedule with Length H

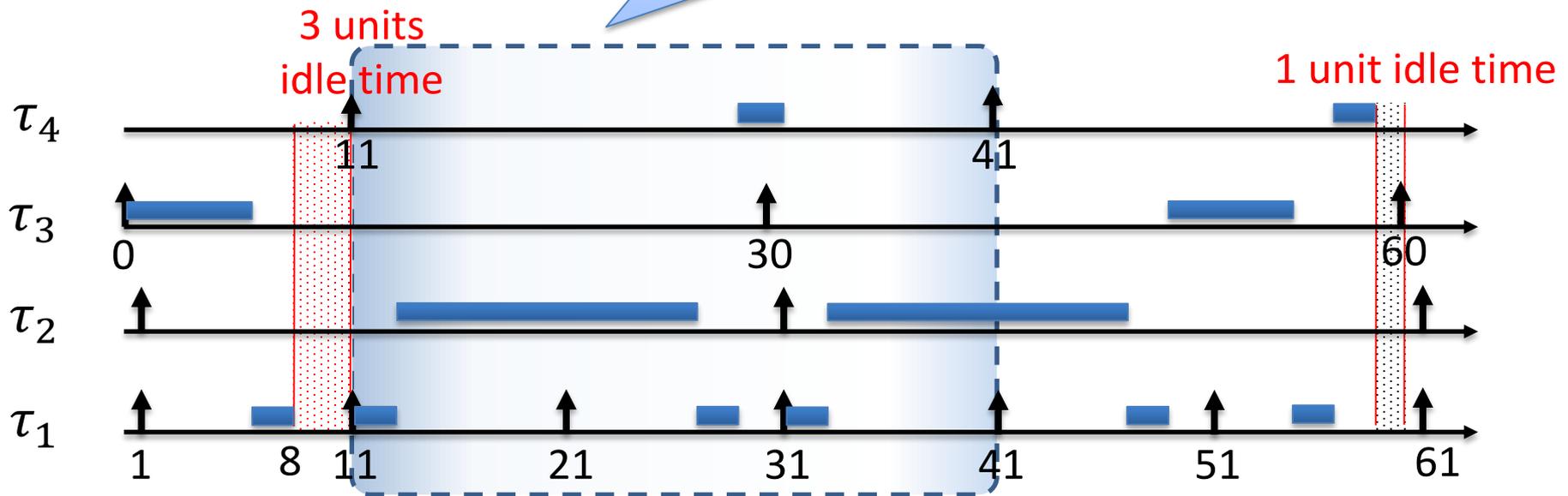
Cannot be a cyclic schedule because  
does not have  $\tau_3$



Hyperperiod =  $H = 30$

# Find a Cyclic Schedule with Length H

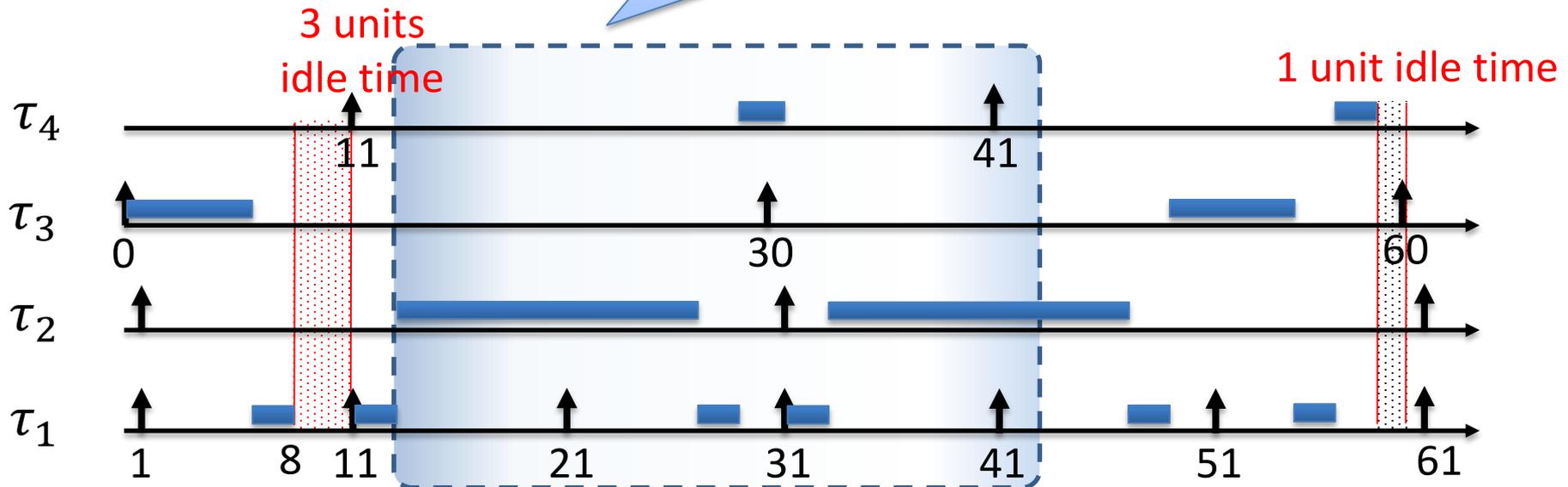
Cannot be a cyclic schedule because does not have  $\tau_3$



Hyperperiod =  $H = 30$

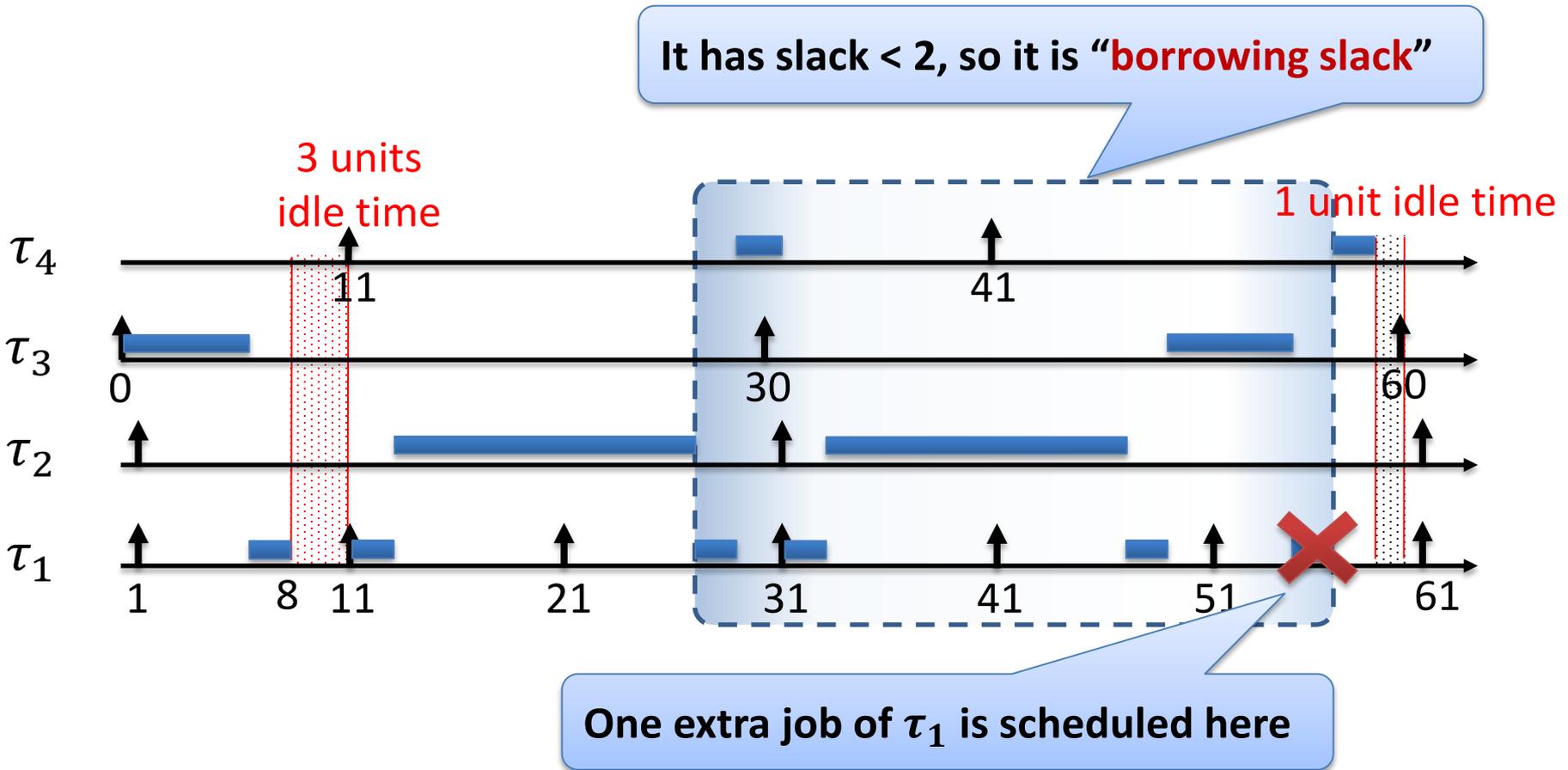
# Find a Cyclic Schedule with Length H

Cannot be a cyclic schedule because  
does not have  $\tau_3$



Hyperperiod =  $H = 30$

# Find a Cyclic Schedule with Length H



Hyperperiod =  $H = 30$

# Non-preemptive Scheduling is a Way to Increase Predictability

- ▶ It increases the predictability
  - Better estimation of the WCET
  - More accurate cache analysis
  - More accurate information about accesses to shared data
- ▶ It is inevitable in many systems
  - GPUs
  - CAN networks
  - small embedded systems
- ▶ It simplifies design and reduces overheads
  - Resource management becomes easier

